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## Wettability, Saturation, and Viscosity Using the Magnetic Resonance Fluid Characterization Method and New Diffusion-Editing Pulse Sequences

R. Freedman, SPE, and N. Heaton, SPE, Schlumberger; M. Flaum, SPE, and G.J. Hirasaki, SPE, Rice University;  
C. Flaum, SPE, and M. Hürlimann, Schlumberger-Doll Research Center

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### Abstract

This paper discusses a new nuclear magnetic resonance (NMR) method that can provide wettability, saturation, and oil viscosity values in rocks partially saturated with oil and brine. The method takes advantage of two new technological advances in NMR well logging — the MRF\* Magnetic Resonance Fluid Characterization Method and NMR “diffusion-editing” (DE) pulse sequences. We discuss the principles underlying the fluid characterization method and the pulse sequences. The fluid characterization method is used to provide robust inversions of DE data suites acquired on fully brine-saturated and partially saturated rock samples. The outputs of the inversion are separate diffusion-free brine and oil  $T_2$  distributions for the fluids measured in the rocks.

NMR measurements on partially saturated rocks are sensitive to wettability because of surface relaxation of the wetting phase fluid. The surface relaxation rate, however, must be significant compared to the bulk relaxation rate in order for wettability to noticeably affect the NMR response. We present results showing that the surface relaxation rate at lower wetting phase saturations is enhanced compared to that measured at higher saturations. The consequence of wetting-phase saturation on NMR-based wettability determination is discussed. Wettability affects the relaxation rates of both the wetting and nonwetting phases in partially saturated rocks. Surface relaxation of the wetting phase in a rock results in shorter relaxation times than would otherwise be observed for the bulk fluid. The nonwetting phase fluid molecules do not

come into contact with the pore surfaces and therefore their relaxation rate in the rock is the same as in the bulk fluid.

We present accurate and robust computations of diffusion-free  $T_2$  relaxation time distributions for both the wetting and nonwetting phases in four rocks that include two sandstones and two dolomites. A DE data suite was acquired on each rock measured in two different partial saturation states and also fully brine saturated. Wettability is determined by comparing the oil and brine  $T_2$  relaxation time distributions measured in the partially saturated rocks with the bulk oil  $T_2$  distribution and with the  $T_2$  distribution of the fully brine-saturated sample. The brine and oil  $T_2$  distributions are used to compute saturation and oil viscosity values.

A general discussion elucidating the sensitivity range and  $T_2$  limits of diffusion-based NMR methods is given in the appendix. The appendix also derives and displays the gain in signal-to-noise ratio that is achieved by using DE data sequences for fluid characterization in place of Carr-Purcell-Meiboom-Gill (CPMG) data suites.

### Introduction

This paper discusses a new nuclear magnetic resonance (NMR) method for determining wettability, saturation, and viscosity values in partially saturated reservoir rocks. It has potential applications to wettability interpretation in native-state cores measured in the laboratory as well as to measurements made downhole by an NMR logging tool. Previous methods for determining wettability of partially saturated rocks, including NMR methods, are limited to laboratory measurements.

NMR wettability determination of partially saturated rocks is based on comparing either  $T_1$  or diffusion-free  $T_2$  distributions of oils *measured in rocks* with the distributions measured on the bulk oils (i.e., outside the rocks). Previous NMR methods of measuring rocks partially saturated with water and oil are only capable of measuring the composite  $T_2$  distribution of both the water and oil phases in the rock. The oil distribution is sometimes measured in restored-state cores by replacing the water phase by  $D_2O$  (heavy water), which does not have an NMR signal at the proton Larmor frequency. The latter approach works well but is not useful for studying

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native-state cores in the laboratory or for downhole NMR measurements.

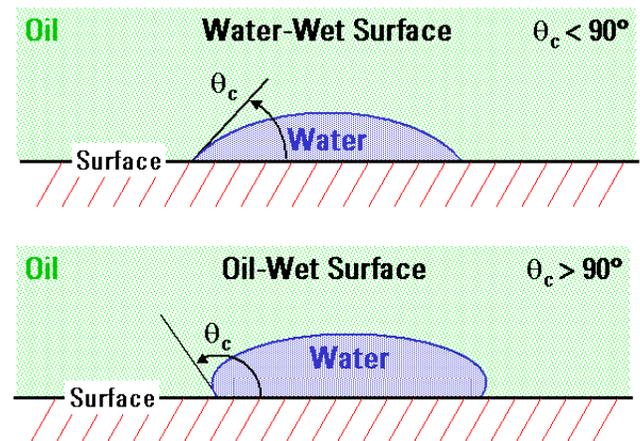
We take advantage of recent innovations in NMR well-logging technology that provide the capability to measure robust and accurate diffusion-free brine and oil  $T_2$  distributions in partially saturated rocks. These innovations are the MRF characterization method and DE pulse sequences.<sup>1-4</sup> The innovations are discussed in detail in the following sections.

The experiments reported on in this paper were conducted at the Schlumberger-Doll Research (SDR) Center. The NMR data were acquired in the fringe field of a superconducting magnet at a proton Larmor frequency of 1.764 MHz with a magnetic field gradient of 13.2 G/cm.

The experiments included measurements on four rocks — Bentheim and Berea sandstones and two dolomite samples from the Yates oil field in west Texas. The samples were partially saturated with a 33°API gravity North Sea stock tank oil. The samples were measured first fully brine saturated and then at two partial saturations. The first partial saturation state was at very high oil saturation achieved by drainage of the brine phase close to residual water saturation. The second partial saturation state was at a lower oil saturation achieved by spontaneous imbibition of water for the sandstones and forced imbibition for the dolomites.

**Wettability.** Wettability is the tendency of a fluid to spread on and preferentially adhere to or “wet” a solid surface in the presence of other immiscible fluids.<sup>5</sup> Knowledge of reservoir wettability is critical because it influences important reservoir properties including residual oil saturation, relative permeability, and capillary pressure. An understanding of the wettability of a reservoir is crucial for determining the most efficient means of oil recovery. This is becoming increasingly important as more secondary and tertiary recovery projects are being undertaken to recover remaining reserves after primary production. It is generally believed that most reservoirs are water wet or mixed wet. The concept of mixed wettability was first introduced by Salathiel.<sup>6</sup> In mixed-wet rocks the brine phase occupies the smaller pores, which are therefore water wet. In the larger oil- and brine-filled pores the oil wets part of the pore surfaces.

Two widely used laboratory indicators of wettability are contact angles measured in water-oil-solid systems and the Amott wettability index. The definition of contact angles and their relationship to wettability is shown in **Fig. 1**. Contact angles less than  $90^\circ$ , measured relative to the water phase, are indicative of a preferentially water-wet surface, whereas angles greater than  $90^\circ$  indicate a preferentially oil-wet surface. A practical limitation of contact angle measurements is that they are restricted to special geometries and cannot be made on reservoir rocks.



**Fig. 1:** The definition of wettability of a brine-oil-solid surface according to the contact angle. If  $\theta_c < 90^\circ$ , water exhibits an affinity for the surface that is said to be preferentially water wet. If  $\theta_c = 0^\circ$ , the surface is strongly water wet. If  $\theta_c > 90^\circ$ , water exhibits an aversion for the surface that is said to be preferentially oil wet. If  $\theta_c = 180^\circ$ , the surface is strongly oil wet.

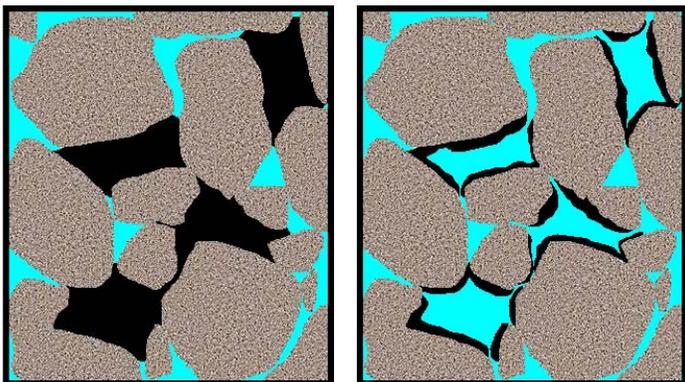
The Amott wettability index is determined from the amount of oil displaced from a core, starting at some initial oil saturation, by spontaneous imbibition of brine divided by the amount of oil displaced by both spontaneous and forced imbibition.<sup>7</sup> Amott defined an analogous index by also considering the displacement of water by oil. The Amott indices vary linearly on a scale from 0 to 1. The endpoints for the displacement of oil by water are 0 for a neutral to oil-wet system and 1 for a strongly water-wet system. Imbibition measurements like the Amott index provide the most quantitative indicators of wettability, however, they are limited to the laboratory.

NMR measurements on fluid-saturated porous media are sensitive to wettability because of the enhanced relaxation rate caused when fluid molecules come into contact with pore surfaces that contain paramagnetic ions or magnetic impurities. Surface relaxation of nuclear magnetism is usually the dominant relaxation mechanism for the wetting phase in a partially saturated rock. The nonwetting phase is unaffected by surface relaxation because the pore surface is coated by the wetting fluid. The other relaxation mechanisms, bulk and diffusion relaxation, affect both the wetting and nonwetting phases. The relaxation rate of the transverse magnetization measured in a spin-echo experiment is the sum of the relaxation rates from all three mechanisms. The bulk relaxation rates for liquids are proportional to their viscosities.

The surface relaxation rate of the wetting-phase in a single pore can be written in the form,

$$\frac{1}{T_{2,\text{surf}}} = \frac{\rho_2 S}{V_{\text{eff}}}, \dots \dots \dots (1)$$

where  $S$  is the surface area of the pore contacted by the fluid of interest and  $\rho_2$  is the surface relaxivity, a parameter that accounts for the effectiveness of the surface in promoting spin-relaxation.  $V_{\text{eff}}$  is the volume occupied by the wetting phase fluid. It can be considerably less than the pore volume especially at low wetting phase saturations. Therefore, in partially saturated rocks, surface relaxation does not depend simply on pore size and surface relaxivity; it is also a function of fluid saturation. For example, in a mixed-wet reservoir at low or residual oil saturation the surface relaxation of the oil is enhanced, compared to that at higher oil saturations, because of the reduced value of  $V_{\text{eff}}$ . Eq. 1 and the discussion regarding the dependence of the surface relaxation effect on oil saturation in a mixed-wet rock have relevance to the experimental results discussed later in this paper. **Fig. 2** shows hypothetical fluid distributions in a mixed-wet rock at initial oil saturation and at after waterflood residual oil saturation.



**Fig. 2:** The fluid distributions in a hypothetical mixed-wet rock at initial oil saturation (left) and at after waterflood residual oil saturation (right). The small pores contain only water and are therefore water wet. The larger oil- and brine-filled pores are oil wet. For the residual oil saturation shown on the right, the volume occupied by the oil ( $V_{\text{eff}}$  in Eq. 1) is small compared with a pore volume. This results in enhanced surface relaxation of the oil compared with the same brine-oil-rock system at higher oil saturation.

**Summary of Previous NMR Wettability Studies.** It is clear from the above discussion that the effects of wettability on NMR surface relaxation can be used to provide information on the wettability state of a fluid-saturated rock.

The first publication using NMR measurements to study wettability was a paper by Brown and Fatt,<sup>8</sup> who made  $T_1$  relaxation measurements on water-saturated unconsolidated sand packs constructed with different fractions of water-wet and oil-wet sand grains. Numerous studies on the application of NMR to wettability have been published since the 1950s. A discussion of many of these papers can be found in the recent paper by Zhang, Huang, and Hirasaki.<sup>9</sup> Many of the previous

studies were conducted on artificial unconsolidated formations.

Studies of wettability of partially saturated reservoir rocks have been mostly limited to rocks saturated with brine and low viscosity hydrocarbons such as Soltrol, decane, and dodecane. Using these low viscosity fluids with narrow  $T_1$  and  $T_2$  distributions and long relaxation times makes it easier to distinguish the hydrocarbon peak from the brine signal in the relaxation time distributions of partially saturated rocks. Thus, by comparison of the hydrocarbon relaxation times in the rocks with those of the bulk hydrocarbon (i.e., outside the rock) one can infer whether the oil is wetting the surface. One of the shortcomings of these experiments is that wettability inferred from experiments using refined or pure hydrocarbons is not indicative of the wettability of the same rocks saturated with crude oil. In fact, crude oils that contain asphaltenes and resins are well known to have surface-active polar molecules that are attracted to opposite charge sites on the pore surfaces.

Zhang *et al.*<sup>9</sup> measured the  $T_1$  distributions of Bentheim, Berea, and North Burbank sandstone rocks using both a 30° API deep-water Gulf of Mexico crude oil and Soltrol as the nonaqueous saturating fluids. This particular crude oil is known to alter wettability in restored-state core analysis. To separate the oil phase from the brine phase in the measured  $T_1$  distributions, the water in the rock was replaced by diffusing D<sub>2</sub>O (heavy water) into the samples. Because D<sub>2</sub>O does not have an NMR signal at the proton Larmor frequency, the signal from just the oil phase in the rock was measured.

Zhang *et al.*<sup>9</sup> found that all three sandstones were water wet when saturated with crude oil and measured at residual water saturation. However, after being aged for 3 weeks at 50°C, the wettability of the samples was changed from water-wet to mixed wet. After aging, the oil peaks for all three samples were shifted to lower relaxation times. Leu *et al.*<sup>10</sup> have recently used high-field NMR spectroscopy and magic angle spinning to study wettability in native-state cores. The proton chemical shift spectrum of the fluids in the rock can be resolved by spinning the sample to average out the line-broadening field inhomogeneities that otherwise smear out the spectrum. The relaxation time distributions of the brine and oil in the rock are separately measured while spinning the sample. This method has value for laboratory work but is not suitable for downhole wettability measurements.

**Fluid Characterization Method.** The new diffusion-based fluid characterization method has been discussed in three recently published papers.<sup>1-3</sup> This method exploits the well-known fact that the decay of the transverse magnetization measured in a spin-echo experiment is due, in part, to molecular diffusion of the fluid molecules. Diffusion of molecules in an inhomogeneous static magnetic field causes the Larmor precession frequencies of the spins to become time dependent. This leads to imperfect refocusing of the spin-echo signals by the 180° pulses, and therefore, to an irreversible diffusion-induced decay of the echoes. The diffusion decay

rate of the transverse magnetization contributed by freely diffusing molecules that contain hydrogen nuclei is given by,

$$\frac{1}{T_{2,diff}} = \frac{\gamma^2 g^2 t_e^2 D}{12}, \dots\dots\dots (2)$$

where  $\gamma = 2\pi \cdot 4258$  Hz/Gauss is the proton gyromagnetic ratio,  $g$  is the magnetic field gradient,  $t_e$  is the echo spacing, and  $D$  is the molecular diffusion coefficient.

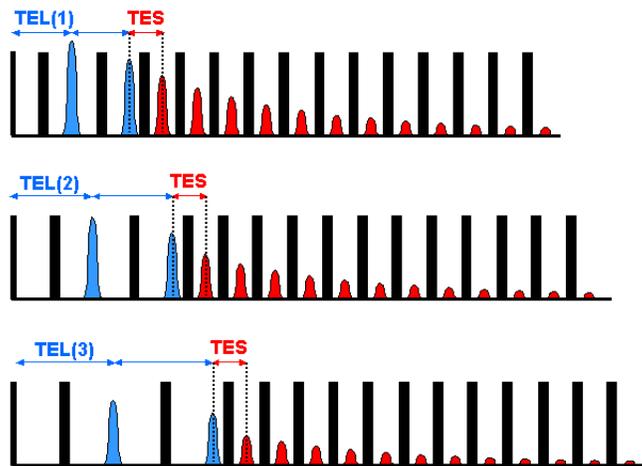
The fluid characterization method performs simultaneous inversions of suites of diffusion-encoded spin-echo sequences. The forward model used for the inversions is a multifluid relaxation model that in general includes contributions to the spin-echo signals from all the fluids that might be present in the rock pore spaces. The inversion provides diffusion-free brine and crude oil  $T_2$  distributions that are used to compute total porosity, bulk volume irreducible water, fluid saturations and volumes, oil viscosity, and hydrocarbon-corrected permeability.

The multifluid relaxation model incorporates a constituent viscosity model (CVM) that relates, on a molecular level, diffusion coefficient distributions ( $D$ ) to relaxation time distributions ( $T_1$  and  $T_2$ ) in live and dead crude oils. The correlation between distributions of relaxation times and molecular diffusion coefficients is used to constrain the inversion. The CVM was validated in experiments on hydrocarbon mixtures including live and dead crude oils.<sup>1</sup> The constrained inversion leads to more robust and accurate computations of both brine and crude oil  $T_2$  distributions in partially saturated rocks than would otherwise be possible.

In the original MRF papers, diffusion information was encoded using suites of CPMG sequences having different echo spacings.<sup>1-2</sup>

**DE Pulse Sequences.** A recent paper by Hürlimann *et al.*<sup>4</sup> introduced, among other things, a new type of “diffusion-edited” (DE) spin-echo sequence tailored for fluid typing. DE sequences are similar to CPMG sequences except that the initial two echoes are acquired with long echo spacings whereas the third and subsequent echoes are acquired with the shortest possible echo spacing. Diffusion information is encoded during acquisition of the first two echoes, whereas the third and subsequent echoes provide bulk and surface relaxation time information at long acquisition times with little if any attenuation of the signal by diffusion. In contrast, a CPMG sequence acquired with long echo spacing provides poorer bulk and surface relaxation time information because diffusion decay attenuates the signal after relatively few echoes. A suite of data consisting of DE sequences acquired with different values for the initial two echo spacings provides diffusion information and improved signal-to-noise ratio compared to an analogous suite of CPMG sequences. A quantitative comparison of the sequences is presented in the appendix. DE sequences provide more accurate and robust computations of brine and oil  $T_2$  distributions in partially saturated rocks than was previously possible. By accurately measuring crude oil  $T_2$  distributions in a rock and comparing

the oil distribution with one measured on the bulk fluid one can infer the wettability state of the rock. A suite of three DE sequences with different state echo spacings for the initial two echoes is shown in Fig. 3.



**Fig. 3: A suite of three fluid typing DE pulse sequences each having different initial echo spacings (TEL) for the first two echoes. The third and subsequent spin-echoes are acquired with the shortest echo spacing possible (TES).**

**MRF Relaxation Model With DE Sequences**

This section of the paper discusses the MRF multifluid relaxation model for DE pulse sequences. For the applications in this paper, we consider a two-fluid MRF model with brine and crude oil. The decay of the transverse magnetization,  $M(t)$ , measured by a DE sequence can be written for a two-fluid model in the general form

$$M(t, t_{e,l}) \approx \sum_{f=o,w} \iiint dD dT_1 dT_2 \left\{ P_f(D, T_1, T_2) \exp\left(-\frac{t}{T_2}\right) I(t, t_{e,l}, D) f(W, T_1) \right\} \dots\dots (3)$$

The sum is over the two fluids, water and oil.  $P_f(D, T_1, T_2)$  is the three-dimensional (3D) diffusion-relaxation time distribution function for each fluid. The function  $f(W, T_1)$  corrects for insufficient recovery time ( $W$ ) between DE sequences, e.g.,

$$f(W, T_1) = 1 - \exp\left(-\frac{W}{T_1}\right) \dots\dots\dots (4)$$

The exponential  $T_2$  decay factor in the integral includes surface relaxation for the wetting phase fluid and bulk relaxation for both fluids. The diffusion kernel for the third and subsequent echoes in the DE sequence was discussed by Hürlimann *et al.*<sup>4</sup> and is given by

$$I(t, t_{e,l}, D) = \left\{ a_d \exp\left(-\frac{\gamma^2 g^2 D t_{e,l}^3}{6}\right) + a_s \exp\left(-\frac{\gamma^2 g^2 D t_{e,l}^3}{3}\right) \right\} \times \exp\left(-\frac{\gamma^2 g^2 D t_{e,s}^2 t}{12}\right) \quad (5)$$

for  $t > 2t_{e,l}$ , where  $t_{e,l}$  is the echo spacing for the initial two echoes (see Fig. 3) and  $t_{e,s}$  is the short echo spacing for the third and subsequent echoes in a DE sequence. The factor containing  $t_{e,s}$  in Eq. 5 accounts for any diffusion-decay occurring during the acquisition of the third and subsequent echoes. Hürlimann<sup>11</sup> has shown that diffusion decay in an inhomogeneous magnetic field is biexponential, with the two contributions coming from direct and stimulated echoes. The direct and stimulated echo coefficients,  $a_d$  and  $a_s$ , depend on the receiver bandwidth of the NMR instrument or logging tool. They can be determined by fitting the diffusion kernel in Eq. 5 to a suite of DE data acquired on a water sample. The values used for all computations in this paper were  $a_d = 0.88$  and  $a_s = 0.04$ . The diffusion kernel for the initial two echoes, (e.g., for  $t \leq 2t_{e,l}$ ) can be represented, to within a very good approximation, by a single exponential decay factor,

$$I(t, t_{e,l}, D) = \exp\left(-\frac{\gamma^2 g^2 D t_{e,l}^2 t}{12}\right). \quad \dots\dots\dots (6)$$

As with CPMG sequences, the first few echoes in a DE sequence are affected by off-resonance effects. These effects can be corrected by multiplying the first few echoes by spin-dynamics correction factors.

Although it is possible, in principle, to invert the DE data suites and extract the 3D diffusion-relaxation time distribution function in Eq. 3, we use the MRF method. This method takes advantage of correlations between relaxation times and diffusion coefficients for crude oils. This provides a huge simplification of the general forward model for DE sequences in Eq. 3 because it reduces the 3D integral for each fluid to a simple one-dimensional (1D) integral over  $T_2$ . For example, the 3D diffusion-relaxation time distribution function for crude oils can be written in the form

$$P_o(D, T_1, T_2) = P_o(T_2) \delta(D - \lambda T_2) \delta(T_1 - \xi_o T_2), \quad \dots\dots\dots (7)$$

where  $P_o(T_2)$  is the diffusion-free  $T_2$  distribution of the oil. The 1D distributions for  $D$  and  $T_1$  are Dirac delta ( $\delta$ ) functions. The parameter  $\lambda$  in Eq. 7 relates the diffusion and relaxation time distributions in accordance with the CVM. For many dead crude oils it has been established that an average value of  $\lambda \approx 1.25 \times 10^{-5} \text{ cm}^2/\text{s}^2$  is appropriate. For live crude oils  $\lambda$  is multiplied by an empirically determined function of the solution gas/oil ratio. The average value of  $\lambda$  given above is determined from the ratio of two empirically derived correlation parameters that relate the log means of diffusion and relaxation time distributions in crude oils to viscosity.<sup>1</sup> Because of the approximate nature of empirical correlations, we have found variations in  $\lambda$ , for different crude oils, of the order of a factor of 2. For the North Sea crude oil used to

saturate the samples in our experiments, it was found that the parameter  $\lambda = 0.51 \times 10^{-5} \text{ cm}^2/\text{s}^2$ . If the wrong value of  $\lambda$  is used then the relaxation model will not fit the data. A poor fit manifests itself in the normalized goodness-of-fit parameter,  $\chi^2$ , being much greater than 1. The correct value of  $\lambda$  for the North Sea oil was found by searching for the value that gave the minimum  $\chi^2$ .

The parameter  $\xi_o$  in Eq. 7 is the  $T_1/T_2$  ratio of the crude oil. It has been established, for Larmor frequencies of a few MHz or less, that  $\xi_o \approx 1$  for many crude oils with low-to-medium viscosities. The  $T_1/T_2$  ratios of crude oils can be greater than 1 for high-viscosity oils and at higher Larmor frequencies because of the breakdown of the fast-motion condition.<sup>1</sup>

The 3D distribution function for the brine phase can be written in the form,

$$P_w(D, T_1, T_2) = P_w(T_2) \delta(D - D_w(T)) \delta(T_1 - \xi_w T_2), \dots (8)$$

where  $D_w(T)$  is the temperature-dependent molecular diffusion coefficient of water and  $\xi_w$  is the apparent  $T_1/T_2$  ratio of the water phase in the rock.

Substituting Eqs. 7 and 8 into Eq. 3 and using the properties of the Dirac delta functions to perform the integrations over  $D$  and  $T_1$ , one finds that the MRF relaxation model for DE sequences can be written as the sum of contributions from the water and oil phases; e.g.,

$$M(t, t_{e,l}) \approx \int dT_2 P_w(T_2) \exp\left(-\frac{t}{T_2}\right) I(t, t_{e,l}, D_w) f(W, \xi_w T_2) + \int dT_2 P_o(T_2) \exp\left(-\frac{t}{T_2}\right) I(t, t_{e,l}, \lambda T_2) f(W, \xi_o T_2). \quad (9)$$

The relaxation model in Eq. 9 was used to invert the suites of DE data for all the experiments discussed in this paper. The details of the inversion follow along the lines previously given by Freedman<sup>12</sup> for suites of CPMG sequences. The inversion provides robust estimates of the water and crude oil  $T_2$  distributions,  $P_w(T_2)$  and  $P_o(T_2)$ .

### Experiments

This section discusses the results of the experiments. We discuss petrophysical properties of the rock samples, crude oil properties, sample preparation, pulse sequences, and the results of the data processing.

**Rock and Crude Oil Properties.** The sandstones used in the experiments were Bentheim (BEN3) and Berea (BER2). The petrophysical properties of these sandstones are quite different. Bentheim is a virtually clay-free rock that has a very high permeability. Berea sandstone is moderately shaly and known to contain kaolinite and illite clays and some localized siderite flakes.

In addition to the sandstones, our experiments included two dolomite rocks (Y1312 and Y1573) from the Yates field in west Texas. The Yates field dolomites have a complex dual-porosity pore space structure that contains significant amounts

of microporosity. The macropores in these rocks include vugs with dimensions of the order of 100 microns. Moreover, these complex rocks are fractured and are also known to be mixed wet from water imbibition experiments. The porosities and permeabilities for the rocks used in the experiments are shown in **Table 1**.

Sample	Porosity (p.u.)	Air Permeabilities (md)
BEN3	23.4	2960
BER2	19.6	205
Y1312	20.8	137
Y1573	14.2	57

Stock tank oil from a North Sea reservoir was used to partially saturate the samples. The properties of the crude oil are shown in **Table 2**.

Oil	API Gravity	Wt% Asphaltenes	Wt% Resins	Wt% Aromatics	Wt% Saturates
N. Sea	33.2	0.0	7.9	24.9	67.1

The measured viscosity of the North Sea crude oil is 9.4 cp at 27°C.

**Sample Preparation and DE Data Suite.** All the core samples were in the shape of 1-in.-long cylinders with 1-in. diameters. The samples were wrapped in heat-shrinkable Teflon, brine saturated by vacuum, and then pressurized to remove any air. A suite of DE measurements was performed on these samples at 100% brine saturation. The samples were then submerged in the North Sea crude oil and centrifuged at 3400 revolutions per minute for 11 hr. The samples were then inverted, and centrifuged for an additional hour. The samples at this stage were close to or at irreducible water saturation and therefore were at high oil saturations. A second suite of DE measurements was then performed. We will refer to this high oil saturation state as the “drainage state” and use the abbreviation “DR” in the following figures and tables. At this point, all the samples were submerged in brine for 16 hr. For the sandstone samples, spontaneous imbibition was observed. For the dolomites, no spontaneous imbibition was observed and the samples were spun in brine at 3400 revolutions per minute for 1 hr to force imbibition. We will refer to this lower oil saturation state as an “imbibition state” and use the abbreviation “IM” in the figures and tables shown below. A final suite of DE data was acquired on the samples in the imbibition state. The NMR measurements were conducted in the fringe field of a superconducting magnet. The samples were placed inside a solenoidal coil tuned to the proton Larmor frequency of 1.76 MHz in a constant magnetic gradient of 13.2 G/cm. The temperature of the samples was held constant at 25°C during the measurements.

The full DE measurement suite acquired on each sample consisted of a CPMG with an interecho spacing of 0.4 ms and

11 DE sequences with initial echo spacings of 1.2, 2.4, 4.4, 8.4, 12.4, 16.4, 20.4, 24.4, 28.4, 32.4, and 36.4 ms. For the DE sequences the short interecho spacing (e.g., for the third and subsequent echoes) was 0.4 ms. The number of echoes acquired for the CPMG and for each DE sequence was 4002. Thus a complete suite of measurements for each sample, including the CPMG, consisted of 48,024 echoes. A polarization time of 6 s preceded each measurement to provide essentially full polarization of all fluids. The sequences for each acquisition were repeated and averaged to reduce the random noise to about 1.0 p.u.

Before discussing the experimental results it is instructive to pause here and display the DE data suites acquired on one of the rock samples measured partially saturated and fully brine saturated. These plots provide insight into why DE data suites are so useful for fluid characterization. **Figs. 4 and 5** show the DE suites for Berea sandstone measured fully brine saturated and partially saturated, respectively. Fig. 4 shows that the water signal decays to the noise level for long initial echo spacings (i.e., TEL) greater than about 20.4 ms. The large attenuation decay for long TEL is due to the large diffusion coefficient of the water molecules. By contrast, there is still signal observed at long TEL in the partially saturated Berea sample shown in Fig. 5. This is because the molecular diffusion coefficients of the molecules in this intermediate viscosity oil are roughly an order of magnitude smaller than that of water. This signal is due entirely to the oil because the water signal decays away during the first two echoes at long TEL. For intermediate viscosity oils, one can qualitatively differentiate a rock that contains oil from one that is fully brine saturated simply by the presence or absence of signal at long values of TEL *without any data processing*.

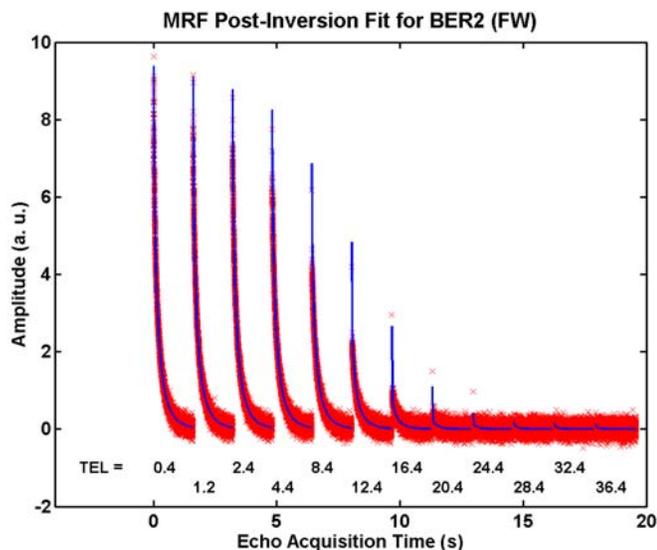


Fig. 4: The full DE data suite acquired on the fully brine-saturated Berea sandstone. The 6-s wait time that preceded each echo acquisition is not shown. The data suite includes a CPMG (the first measurement shown) with an echo spacing of 0.4 ms. Observe that the water signal has decayed to the noise level for TEL greater than about 20.4 ms. The water signal decays rapidly to the noise level at long TEL because of the large diffusion coefficient of water. The fact that no signal is observed for long TEL is a good indicator that the sample is water saturated. The solid lines are the post-inversion fit of the relaxation model to the full DE data suite.

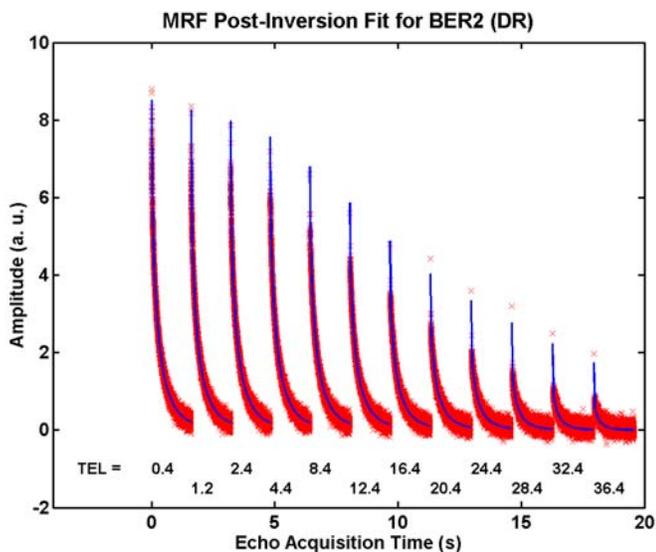


Fig. 5: The full DE data suite acquired on the Berea sandstone measured in the drainage state. The 6 s wait time that preceded each echo acquisition is not shown. The data suite includes a CPMG (the first measurement shown) with an echo spacing of 0.4 ms. Observe that there is observable signal for all the DE measurements. The signal observed at long TEL is due to oil only, because the more rapidly decaying water signal disappears for TEL greater than about 20.4 ms. The solid lines are the post-inversion fit of the relaxation model to the full DE data suite.

**Fully Brine-Saturated Samples.** The  $T_2$  distributions for the North Sea Oil and each of the rocks at 100% brine saturation were first measured using the CPMG sequence. These distributions are shown in Fig. 6. Note that the brine  $T_2$  distributions all strongly overlap the crude oil distribution. This strong overlap of brine and oil  $T_2$  distributions in partially saturated rocks makes it difficult to accurately differentiate and separate brine and oil distributions in the composite  $T_2$  distributions that contain both brine and oil.

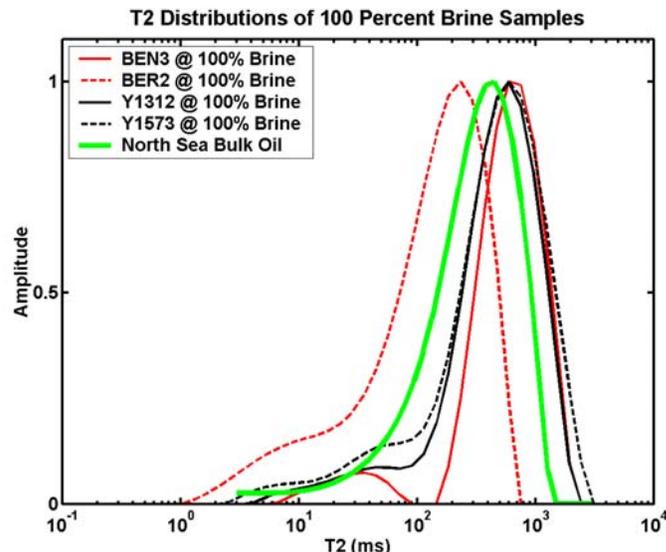
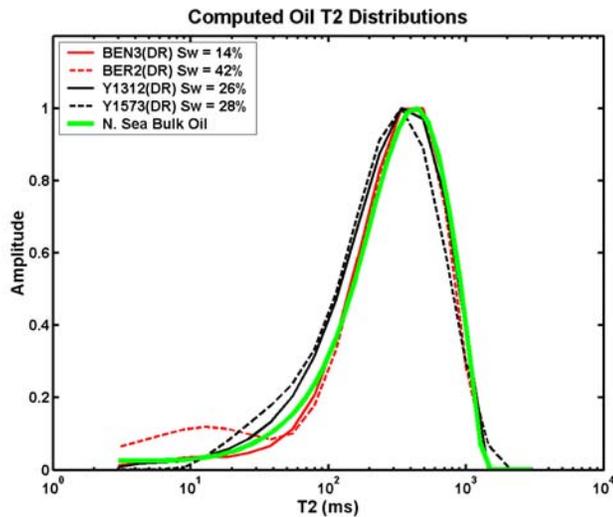


Fig. 6: The  $T_2$  distributions of the North Sea crude oil and the 100% brine-saturated rocks measured using the CPMG sequence. Note the strong overlap of the oil and brine  $T_2$  distributions. It is this overlap between oil and brine  $T_2$  distributions in partially saturated rocks that makes it difficult to accurately separate the oil and brine phases.

#### Wettability Results for the Partially Saturated Samples.

Fig. 7 shows diffusion-free oil  $T_2$  distributions computed from the fluid characterization method by inversion of the DE data suites acquired for each of the partially saturated rocks in the drainage state. The computed water saturations are also shown. Also shown is the  $T_2$  distribution of the North Sea bulk oil. Note that the oil  $T_2$  distribution measured “in each of the rocks” agrees very well with the bulk distribution for the oil measured “outside the rocks.” The oil distributions measured in the two Yates samples show a very slight shift to shorter relaxation times. Nevertheless, one would conclude from Fig. 7 that all four of these partially saturated rocks are water wet because there is no conclusive evidence of surface relaxation of the oil phase. This conclusion is incorrect because in fact the two Yates samples are mixed wet. The reason that surface relaxation of the oil measured in these samples is not evident is that the surface relaxation rate depends on the saturation of the wetting phase, as is discussed in the paragraph that follows Eq. 1. Because these samples were measured at high oil saturations, the surface relaxation rate is too weak in comparison to the bulk relaxation rate to produce a noticeable effect.

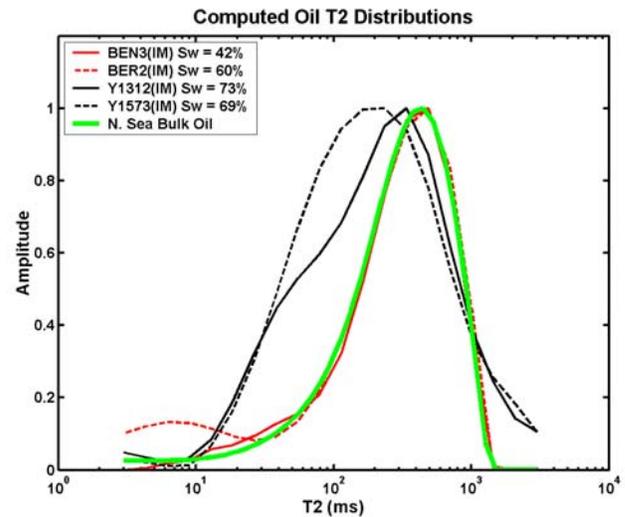


**Fig. 7:** The diffusion-free oil  $T_2$  distributions computed by the fluid characterization method for the samples measured in the drainage state compared with the bulk oil distribution. Note that there is no convincing evidence of surface relaxation of the oil phase even though the two Yates samples are mixed wet. The surface relaxation rate of the oil is not significant compared to the bulk oil relaxation rate at these high oil saturations.

The dependence of the surface relaxation rate on wetting phase saturation is evident in **Fig. 8**, which shows computed oil distributions for the samples measured in the imbibition state. In Figs. 7 and 8 note that the water saturations in the imbibition state are significantly higher than those measured after drainage. The oil  $T_2$  distributions measured in the two Yates samples in the imbibition state show a significant shift towards shorter relaxation times. This effect is due to surface relaxation of the oil in these mixed-wet dolomites that is enhanced because of the higher water saturations. Fig. 8 shows that the oil distributions computed for the two water-wet sandstones, BEN3 and BER2, agree very well with the bulk oil distribution and show no signs of surface relaxation.

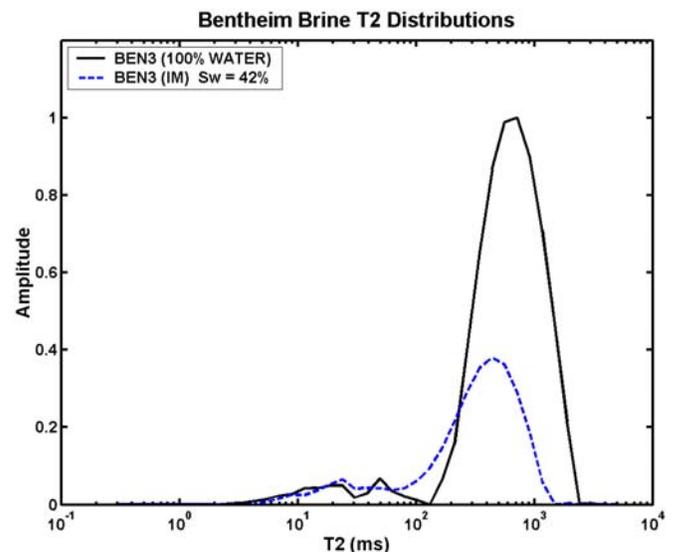
It is clear from the above results that oil relaxation time distributions measured in mixed-wet rocks with oil in contact with the pore surface can show signs of significant surface relaxation. However, if no surface relaxation of oil in a rock is observed, one cannot conclude that the rock is water wet; however if one observes a significant shift towards short relaxation times of the oil  $T_2$  distribution compared to that of the bulk oil, one can conclude that the rock is mixed wet. These observations place some qualifications, not previously discussed in the literature, on the sensitivity of NMR measurements to wettability.

Wettability has an effect on both the wetting and nonwetting fluids in a pore. The relaxation rate of the wetting fluid is increased by surface relaxation at the pore surface, whereas the relaxation rate of the nonwetting fluid should approach its bulk value because there is no surface relaxation effect. In light of these remarks, it is instructive to compare the computed brine distributions for the samples measured in the imbibition state with those measured fully brine saturated.



**Fig. 8:** The diffusion-free oil  $T_2$  distributions computed by the fluid characterization method for the samples measured in the imbibition state compared with the bulk oil distribution. Note that there is convincing evidence of surface relaxation of the oil phase in the two mixed-wet Yates samples.

**Figs. 9 and 10** show the brine  $T_2$  distributions for the Bentheim and Berea sandstones measured at imbibition and at 100% brine saturation. The brine distributions are consistent with one's expectations for a water-wet rock. At imbibition brine and oil occupy the larger pores and the smaller pores are filled with brine. Because the rock is water wet, the brine in the larger pores remains in contact with the pore surfaces. The brine relaxation times in the large pores are reduced compared to those of the fully brine saturated rock because the effective volume of the brine in the larger pores is reduced (e.g., see Eq. 1) by the presence of the oil.



**Fig. 9:** Comparison of the brine distributions for the Bentheim sandstone measured fully brine saturated and in the imbibition state. As discussed in the text, these distributions are consistent with those expected for a water-wet rock.

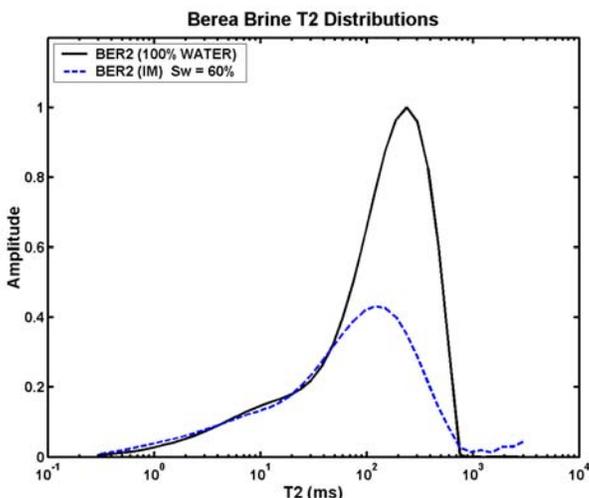


Fig. 10: Comparison of the brine distributions for the Berea sandstone measured fully brine saturated and in the imbibition state. As discussed in the text, these distributions are consistent with those expected for a water-wet rock.

Figs. 11 and 12 show the brine  $T_2$  distributions for the Yates dolomites measured at imbibition and at 100% brine saturation. The brine distributions for these rocks measured in the imbibition state are consistent with that of a mixed-wet rock with brine occupying the small pores and oil wetting the pore surfaces in the larger pores (e.g., see Fig. 2). In the imbibition state the brine in the larger pores does not contact the pore surfaces and therefore relaxes with its bulk relaxation time. This is exactly the behavior observed in Figs. 11 and 12. Note how the centers of the brine distributions measured at imbibition are shifted to longer relaxation times. This behavior is quite different from that observed in Figs. 9 and 10 for the water-wet sandstones.

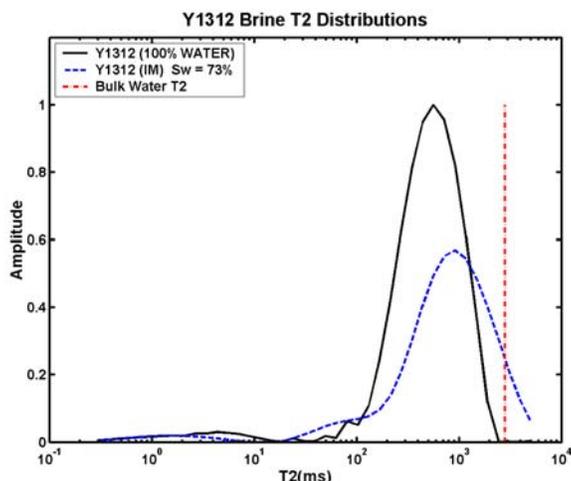


Fig. 11: Comparison of the brine distributions for the Y1312 dolomite sample measured fully brine saturated and in the imbibition state. Note that some of the brine in the large oil- and brine-filled pores is not in contact with the pore surfaces and therefore relaxes close to its bulk rate. In the fully brine-saturated state the brine relaxation times in the large pores are reduced compared to that of bulk brine by surface relaxation.

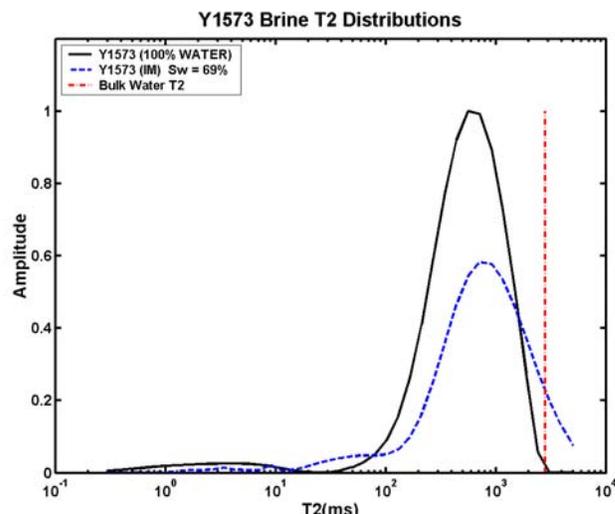
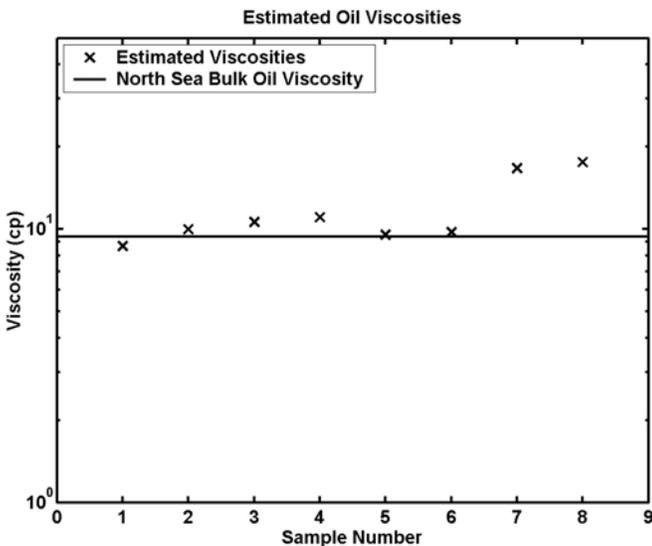


Fig. 12: Comparison of the brine distributions for the Y1573 dolomite sample measured fully brine saturated and in the imbibition state. Note that some of the brine in the large oil- and brine-filled pores is not in contact with the pore surfaces and therefore relaxes close to its bulk rate. In the fully brine-saturated state the brine relaxation times in the large pores are reduced compared to that of bulk brine by surface relaxation.

**Saturation and Viscosity Results.** Table 3 lists some results obtained from MRF processing of the DE data suites for each of the 8 partially saturated samples measured in this study. Column 1 lists the samples and shows the saturation state at which each measurement was performed. Column 2 lists the computed water saturations. Column 3 lists the log means of the computed oil  $T_2$  distributions. The log mean of the  $T_2$  distribution of the North Sea bulk oil sample is 288 ms and the measured viscosity at 27°C is 9.4 cp. The log means of the oil distributions in the partially saturated samples are, except for Y1312 (IM) and Y1573 (IM), in good agreement with that of the bulk oil. Fig. 13 shows the estimated viscosities that are derived from the log means using an empirical correlation.<sup>1</sup> The agreement with the measured viscosity is very good except for the two Yates samples measured at imbibition. For these two mixed-wet samples surface relaxation reduces the log mean relaxation times compared to that of the bulk oil and causes over estimation of the viscosity. For the North Sea oil used in these experiments, the empirically derived parameter that relates the log mean of the oil distribution to viscosity is equal to  $0.0087 \text{ s}\cdot\text{cp}\cdot\text{K}^{-1}$  which is 2.17 times greater than the default value frequently used for crude oils.<sup>1</sup> Also the parameter that relates oil diffusion coefficients to relaxation times in the CVM has the value  $\lambda = 0.51 \times 10^{-5} \text{ cm}^2/\text{s}^2$  which also deviates from the default value. Column 4 lists the normalized the goodness-of-fit parameter ( $\chi^2$ ) computed after the inversion. A value equal to 1.0 (or less) indicates a perfect fit to within noise errors.

Sample	$S_w$ (%)	$T_{2O,LM}$ (ms)	$\chi^2$
BEN3 (DR)	13.8	297	0.97
BER2 (DR)	42.0	257	1.06
Y1312 (DR)	26.1	243	1.02
Y1573 (DR)	28.4	235	0.99
BEN3 (IM)	42.4	273	0.99
BER2 (IM)	60.3	266	1.06
Y1312 (IM)	73.3	155	1.01
Y1573 (IM)	69.1	147	1.01

The correlation between  $D$  and  $T_2$  in Eq. 7 was developed for bulk crude oils. In mixed-wet rocks, with significant surface relaxation of the oil phase, the  $T_2$  values of the oil can be substantially reduced compared with their bulk values. If the diffusion constants remained unchanged, this would imply a deviation from the bulk oil correlation. The fact that the model provides a good fit to the data in the mixed-wet rocks, Y1312 (IM) and Y1573 (IM), suggests that the oil diffusion constants are also reduced. Apparently, at high water saturations, the oil molecules are trapped in the thin layers between the grain surfaces and the oil/water interfaces and experience restricted diffusion. As was shown in a previous publication, the model also provides accurate estimates of fluid saturations in mixed-wet rocks.<sup>2</sup>



**Fig. 13:** The estimated viscosities for the 8 partially saturated samples listed in Table 3. The sample number on the x-axis is consistent with the order in which the samples are listed in Table 3. The good agreement with the measured bulk oil viscosity for Samples 1 through 6 is due to accurate estimations of the  $T_2$  distributions of the oil in the rocks and the absence of significant surface relaxation effects. The overestimation of the viscosity for the two Yates samples measured at imbibition is caused by the significant surface relaxation of the oil in these mixed-wet rocks.

**Table 4** shows estimated water saturations and normalized goodness-of-fit parameters for the samples measured in the fully brine-saturated state. The notation “FW” is used to indicate that the samples were fully brine saturated. The underestimation (i.e., by a few saturation percent) of the water saturations in the sandstone samples is caused by model and data errors. This is within the expected accuracy limits of the technique. The bigger underestimation of the water saturation in the Yates samples is caused, in part, by restricted diffusion of the brine molecules in the microporosity. Restricted diffusion can cause water trapped in the micropores to be mistaken for oil molecules. For these molecules the apparent diffusion coefficients are reduced and clearly depend on the sizes of the micropores and therefore on their  $T_2$  values. Another reason for errors in the water saturation is the lack of diffusion sensitivity at very short relaxation times that makes it impossible to reliably differentiate water in micropores from fast-relaxing constituents in crude oils.

Sample	$S_w$ (%)	$\chi^2$
BEN3 (FW)	95.7	0.97
BER2 (FW)	96.2	1.10
Y1312 (FW)	91.7	1.03
Y1537 (FW)	83.2	1.02

## Conclusions

This paper discussed a new NMR method for measuring wettability, saturation, and viscosity in rocks partially saturated with brine and crude oils. The method has advantages over existing methods for determining wettability. In particular, the method presented here is applicable to analysis of native-state cores and also to downhole determination of wettability.

The sensitivity of NMR measurements to the wetting phase saturation was discussed and demonstrated using data acquired from two mixed-wet dolomite samples measured at different oil saturations.

We demonstrated that the fluid characterization method can be combined with DE pulse sequences to provide more robust fluid characterization than was previously possible. The DE pulse sequences were shown to provide a clear advantage over CPMG sequences for fluid characterization.

## Acknowledgments

We thank Drs. Francois Auzerais and Martin Poitzsch for supporting this study. We are also grateful to the oil companies that provided the core and oil samples used in the experiments.

## Nomenclature

- $a_d$  = amplitude of direct echo contribution (see Eq. 5)  
 $a_s$  = amplitude of stimulated echo contribution (see Eq. 5)  
 $D$  = diffusion coefficient,  $\text{cm}^2 \cdot \text{s}^{-1}$   
 $g$  = applied magnetic field gradient, G/cm  
 $I(t, t_e, b, D)$  = diffusion kernel for DE pulse sequence (see Eqs. 5 and 6)  
 $j$  = integer index that denotes echo number  
 $M(t, t_e, i)$  = transverse magnetization in DE sequence, p.u.  
 $P(D, T_1, T_2)$  = 3-d diffusion-relaxation time distribution, (p.u.) ·  $\text{cm}^{-2} \cdot \text{s}^{-1}$   
 $P(T_2)$  =  $T_2$  distribution, (p.u.) ·  $\text{s}^{-1}$   
 $p$  = integer index that denotes measurement number in a suite of DE measurements  
 $S$  = surface area of a pore in contact with the wetting fluid of interest,  $\text{cm}^2$   
 $T_1$  = longitudinal relaxation time, s  
 $T_2$  = diffusion-free spin-spin relaxation time caused by surface and bulk relaxation, s  
 $T_{2,\text{surf}}$  = spin-spin relaxation time caused by surface relaxation, s  
 $T_{2,\text{diff}}$  = spin-spin relaxation time caused by molecular diffusion in the applied magnetic field gradient, s  
 $t$  = echo acquisition time, s  
 $t_e$  = echo spacing, s  
 $t_{e,l}$  = long echo spacing for initial two echoes in DE sequence, s  
 $t_{e,s}$  = short echo spacing for third and subsequent echoes in DE sequence, s  
 $V_{\text{eff}}$  = volume of the wetting phase in a rock pore,  $\text{cm}^3$   
 $W$  = wait time preceding a DE or CPMG measurement, s  
  
 $\gamma$  = proton gyromagnetic ratio,  $(\text{Gauss} \cdot \text{s})^{-1}$   
 $\xi$  = apparent  $T_1/T_2$  ratio of oil or water  
 $\rho_2$  =  $T_2$  surface relaxivity,  $\text{cm} \cdot \text{s}^{-1}$   
 $\lambda$  = parameter that relates diffusivity and relaxation time in a crude oil,  $\text{cm}^2 \cdot \text{s}^{-2}$   
 $\chi^2$  = normalized goodness-of-fit parameter used to assess how well the MRF relaxation model fits the DE data suite

## Subscripts:

- $o$  = oil  
 $w$  = brine  
 $f$  = oil or brine

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**Appendix:  $T_2$  Sensitivity Limits of NMR-Based Fluid Characterization and Comparison of DE and CPMG Data Suites**

The fluid characterization method relies on the fact that signals from water and crude oil usually have different diffusion attenuation rates because of contrasts in their molecular diffusion coefficients. The method also requires that the NMR signal relaxation rate caused by diffusion is significant in comparison to other relaxation processes; i.e., surface and bulk relaxation. The latter requirement is not satisfied for very viscous oils or for very fast relaxing brine signals for which there can be negligible sensitivity to diffusion relaxation. This lack of diffusion information means that NMR cannot reliably differentiate fast-relaxing water in small pores or clay bound waters from heavy constituents in crude oils that also have very short relaxation times. This limitation applies to all NMR-based diffusion methods and was discussed in a previous paper.<sup>2</sup> At the other end of the spectrum, NMR diffusion methods cannot reliably differentiate bulk water in large pores from very low viscosity oils with similar diffusion coefficients. In the latter cases, the problem is not due to insignificant diffusion relaxation. Indeed, for both light oils and bulk water the diffusion attenuation rates are high. The problem is caused by lack of contrast between the diffusion coefficients of very low viscosity oils and water.

In this appendix, we quantify the aforementioned limits by a simple sensitivity analysis of the errors in the volume estimates of water and crude oil in a partially saturated rock. The computations also show that suites of DE sequences provide more robust and accurate fluid volumes than can be obtained using suites of CPMG sequences.

To simplify the computations, we will assume that the rock is water wet and that the measurements are all fully polarized. Consider a fixed value of  $T_2$  caused by bulk and surface relaxation for the water and by bulk relaxation for the oil. Consider a suite of DE sequences and let  $M_k$  be the amplitude of the measured transverse magnetization. To save space, we have introduced the dual-index  $k = (j,p)$  where  $j$  is the echo number and  $p$  denotes a DE sequence in the measurement suite. In the following analysis, summations over the index  $k$  are understood to be a double summation over all echoes in each sequence and then over all sequences in the suite. On using Eq. 9, the measured magnetization  $M_k$  for the  $j$ th echo and  $p$ th DE sequence can be written in the form

$$M_k = V_o \exp\left(-\frac{j t_{e,k}}{T_2}\right) I(k, \lambda T_2) + V_w \exp\left(-\frac{j t_{e,k}}{T_2}\right) I(k, D_w(T)) \quad , \dots\dots\dots (A-1)$$

where  $V_o$  and  $V_w$  are the volumes of oil and water with relaxation time  $T_2$ . The echo spacings  $t_{e,k}$  for DE sequences depend on both echo and sequence number, i.e.,

$$t_{e,k} = t_{e,jp} \quad \text{for } j=1,2 \quad , \dots\dots\dots (A-2)$$

$$t_{e,k} = t_{e,s} \quad \text{for } j \geq 3 \text{ for all } p$$

where  $t_{e,s}$  and  $t_{e,jp}$  are the short echo spacing for the third and subsequent echoes and the measurement-dependent initial echo spacings, respectively, used in the DE data suite.

Least-squares estimates of the fluid volumes and the errors in the volumes can be found by minimization of the squared deviations of the measured echo amplitudes from the model values. That is, one minimizes the error function  $E(V_o, V_w)$ ,

$$E(V_o, V_w) = \sum_k (M_k - V_o M_o(k) - V_w M_w(k))^2 \quad , \quad (A-3)$$

where the quantities  $M_o(k)$  and  $M_w(k)$  are defined by the equations

$$M_o(k) = \exp\left(-\frac{j t_{e,k}}{T_2}\right) I(k, \lambda T_2) \quad \dots\dots\dots (A-4)$$

and,

$$M_w(k) = \exp\left(-\frac{j t_{e,k}}{T_2}\right) I(k, D_w(T)) \quad \dots\dots\dots (A-5)$$

Setting the first partial derivatives of  $E(V_o, V_w)$  with respect to  $V_o$  and  $V_w$  equal to zero leads to the least-squares solution

$$V = A^{-1} * Q \equiv U * Q \quad , \quad \dots\dots\dots (A-6)$$

where we defined the column vectors  $V = (V_o \ V_w)^T$  and  $Q = (Q_o \ Q_w)^T$ . The asterisk (\*) denotes matrix multiplication and the superscript "T" denotes the transpose. The components of the  $Q$  vector are explicitly given by the equations,

$$Q_o = \sum_k M_k M_o(k) \quad \dots\dots\dots (A-7)$$

and,

$$Q_w = \sum_k M_k M_w(k) \quad . \quad \dots\dots\dots (A-8)$$

The elements of the 2x2 matrix  $A$  in Eq. A-6 are given by the equations

$$A_{1,1} = \sum_k M_o^2(k) \quad \dots\dots\dots (A-9)$$

$$A_{1,2} = A_{2,1} = \sum_k M_o(k) M_w(k) \quad \dots\dots\dots (A-10)$$

and,

$$A_{2,2} = \sum_k M_w^2(k) \quad . \quad \dots\dots\dots (A-11)$$

The matrix  $U$  in Eq. A-6 is the inverse of  $A$ . To save space, we do not display the matrix elements of  $U$ , which are easily calculated. Using the above results the estimated volumes of water and oil having relaxation time  $T_2$  are given by,

$$V_o = U_{1,1} Q_o + U_{1,2} Q_w \quad \dots\dots\dots (A-12)$$

$$V_w = U_{1,2} Q_o + U_{2,2} Q_w \quad . \quad \dots\dots\dots (A-13)$$

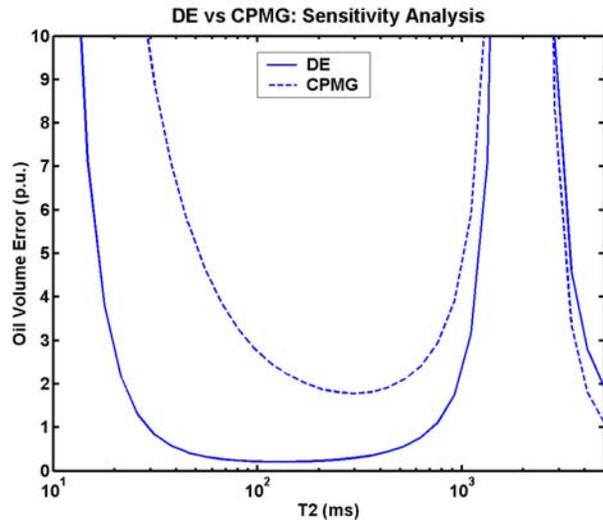
The standard deviations or errors in the estimated volumes are easily obtained from the above equations. The errors come from the measurements  $M_i$  and therefore from the vector  $Q$  in Eqs. A-12 and A-13. If we denote the noise per echo for all the measurements by  $\sigma_0$  and take the variance of both sides of the above equations, we find that the standard deviations in the oil and water volumes are given by,

$$\sigma(V_o) = \sigma_0 [U_{1,1}^2 A_{1,1} + U_{1,2}^2 A_{2,2}]^{0.5} \dots\dots (A-14)$$

$$\sigma(V_w) = \sigma_0 [U_{1,2}^2 A_{1,1} + U_{2,2}^2 A_{2,2}]^{0.5} \dots\dots (A-15)$$

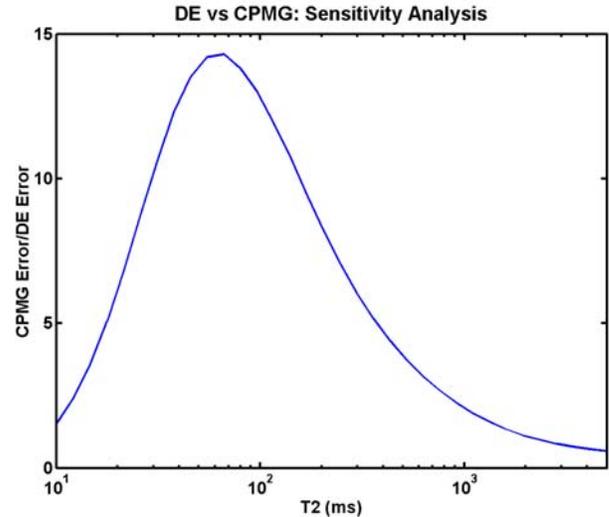
In arriving at the above results we have assumed that the noise on different echoes is uncorrelated.

The errors in the volume estimates have been computed for suites of DE and CPMG sequences. **Fig. A-1** shows a comparison of the standard deviations in the oil volumes as a function of  $T_2$  for suites of DE and CPMG data. The standard deviations shown in Fig. A-1 were computed for data with 1.0 p.u. of random noise. The DE data suite used for the experiments in this paper was used for the computations. A CPMG data suite with echo spacings similar to those used in the DE suite was used for the computations. A gradient of 13.2 G/cm and a temperature of 25°C were used. It is clear from Fig. A-1 that there are large errors in the estimated oil volumes for both short and long  $T_2$  for the reasons discussed at the beginning of this appendix. The errors are smaller for the DE data suite than for the CPMG suite for the reasons discussed in the paper. Observe that the errors actually decrease for very long  $T_2$ . The reason is that this is the regime of very light oils and condensates. There is good diffusion contrast because hydrocarbon diffusivities can be significantly greater than that of water for very long  $T_2$  values.



**Fig. A-1:** Plot showing the standard deviations in the estimated oil volumes as a function of diffusion-free  $T_2$  for suites of DE and CPMG data. A noise per echo of 1.0 p.u. was used in the computations.

**Fig. A-2** shows the ratio of the oil volume error for the CPMG data suite to the error for the DE data suite as a function of diffusion-free  $T_2$ . This ratio represents the “gain” in measurement signal-to-noise ratio that is achieved from using DE data suites in place of CPMG data suites.



**Fig. A-2:** The gain in measurement signal-to-noise ratio as a function of diffusion-free  $T_2$  achieved by using DE data suites in place of CPMG data suites.

**SI Metric Conversion Factors**

°API	141.5/(131.5 + °API)	= g/cm
cp	x 1.0* E - 03	= Pa · s
cycles/s	x 1.0* E + 00	= Hz
ft	x 3.048* E - 01	= m
°F	(°F + 459.67)/1.8	= K
in.	x 2.54* E + 00	= cm

\*Conversion factor is exact.